Phys 410

Fall 2013

Homework #0

Due Thursday, 5 September, 2013

Complete the following by hand (no assistance from computers!):

- 1. Use the Euler formula to expand $e^{i\theta}$ for real θ .
- 2. Given the three Cartesian unit vectors \hat{x} , \hat{y} , and \hat{z} , calculate the following:
 - a. $\hat{x} \times \hat{y}$
 - b. $|\hat{x}|$
 - c. $\hat{x} \cdot \hat{y}$
- 3. Given the vectors $\vec{r} = (r_x, r_y, r_z)$ and $\vec{s} = (s_x, s_y, s_z)$, calculate the cross product vector $\vec{r} \times \vec{s}$ in terms of its Cartesian components.
- 4. Find the eigenvalues and eigenvectors of this matrix: $\bar{A} = \begin{pmatrix} 1 & 2 \\ 2 & 1 \end{pmatrix}$.
- 5. What is the determinant of $\overline{\overline{A}}$ and how is it related to the eigenvalues?
- 6. What is the trace of \overline{A} and how is it related to the eigenvalues?
- 7. Given a scalar function of position $\chi(\vec{r})$ (e.g. the temperature distribution on the surface of the earth), what can we say is always true about the curl of the gradient of χ ?
- 8. Given a vector field $\vec{F} = k(x, 2y^2, 3z^3)$, where k is a constant, calculate its curl, $\nabla \times \vec{F}$.
- 9. What is the general solution to the second-order linear differential equation $\ddot{x} = -\omega^2 x$, where ω is a real positive number?
- 10. What is the general solution to the second-order linear differential equation $\ddot{x} = +k^2 x$, where k is a real positive number?
- 11. Given ln(y) = b ln(x), where b is a constant, find y as a function of x, y(x).
- 12. Evaluate the integral $I = \int_{-2}^{3} 5x \, dx$.
- 13. Write down the differential volume element d^3r in spherical coordinates. Use the figure below for definition of the spherical coordinates.

